

# Using Small-Scale History Data to Predict Large-Scale Performance of HPC Application

Wenju Zhou

University of Science and Technology  
of China

2020.05.12

USTC

# Outline

---

- ◆ Background
- ◆ Two-level model
- ◆ Experiment results and analysis
- ◆ Conclusions

# 01 | Background

# High Performance Computing (HPC)

- architecture:  
computing nodes,  
interconnect, ...
- usage:  
physical simulations,  
molecular modeling, ...
- effect:  
provide computing power,  
reduce experimental risk, ...

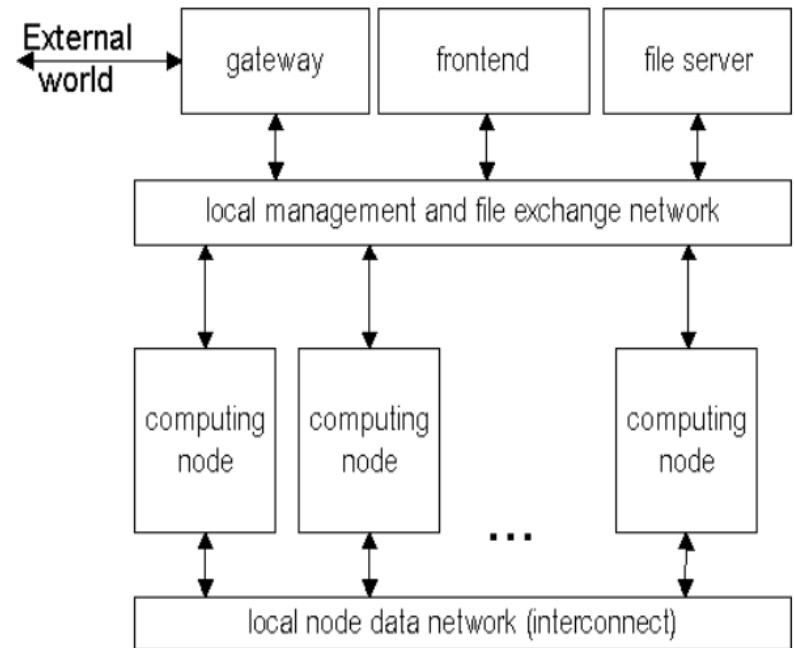


fig 1. architecture of HPC

# Performance Modeling

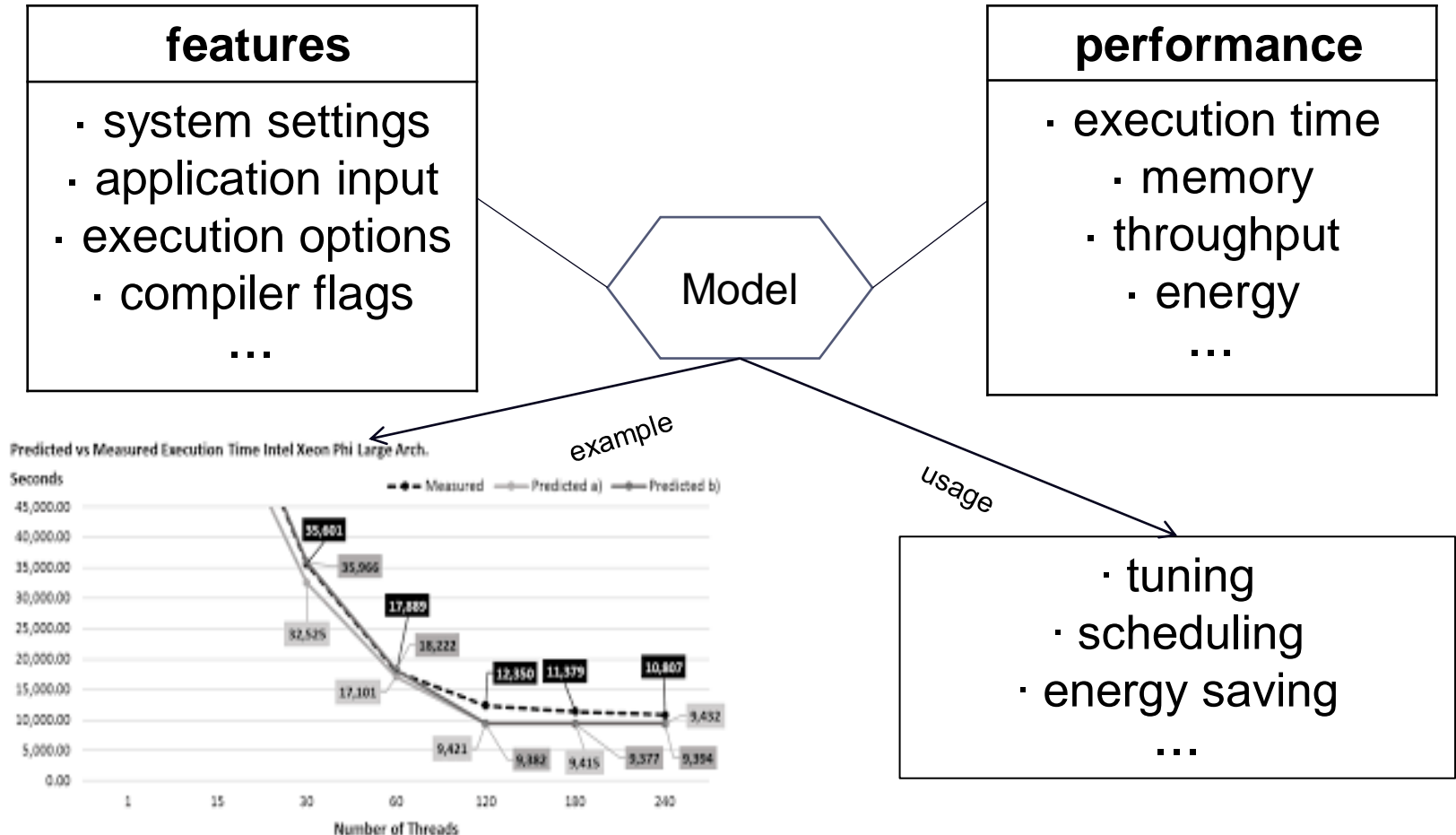


fig 2. architecture of HPC

# Performance Modeling

---

categories	description	advantaes	limitations
simulative methods	simulating execution by simulators	concept machine	overhead
analytical methods	analysis of code and system by experts	accuracy & Interpretability	overhead
empirical methods	statistical analysis of historical data	automation	cold start

- system complexity
- application complexity
- interaction between system and application

attention on  
empirical methods

# Machine Learning in Performance Modeling

---

Machine Learning	
A technology to learn knowledge and experience from historical data.	A powerful approach for empirical modeling methods.

- D. N. Hieu, T. T. Minh, T. Van Quang, B. X. Giang, and T. Van Hoai, “A machine learning-based approach for predicting the execution time of cfd applications on cloud computing environment,” in International Conference on Future Data and Security Engineering, pp. 40–52, Springer, 2016
- P. Malakar, P. Balaprakash, V. Vishwanath, V. Morozov, and K. Kumaran, “Benchmarking machine learning methods for performance modeling of scientific applications,” in 2018 IEEE/ACM Performance Modeling, Benchmarking and Simulation of High Performance Computer Systems (PMBS), pp. 33–44, IEEE, 2018.

# Extrapolation Issue of Machine Learning

---

- Extrapolation:  
testset feature subspace outside trainset feature subspace.
- Issue  
high-accuracy interpolations but low-accuracy extrapolations — machine learning can achieve high-accuracy predictions in trainset subspace, but prediction accuracy reduces drastically outside trainset subspace.



**02**

Two-level Model

# Problem Description

---

## Features

$X: (x_1, x_2, x_3, \dots, x_n, p)$

input parameters,  
Identically and  
Independent  
Distributed in  
 $X_{train}$  and  $X_{test}$ .

number of  
processors,  
 $p \in [a, b]$  in  $X_{train}$ ,  
 $p \in [c, d]$  in  $X_{test}$ ,  
 $b < c$ .

## Label

$y$

execution time,  
 $y_{train}$  is known  
from historical  
logs,  $y_{test}$  is to  
be predicted.

# Machine Learning Mechanism

---

Target model:

$$f^* = \arg \min_f L(y_{test}, f(X_{test}))$$

Independent and  
Identically Distributed  
(IID) hypothesis

Approximate model:

$$f^* \approx \arg \min_f L(y_{train}, f(X_{train}))$$

# Motivation of Two-Level Model

---

Issues of one-level model	Overview of two-level model
<ul style="list-style-type: none"><li>- Simple algorithms:<ul style="list-style-type: none"><li>· own extrapolation ability in some way</li><li>· cannot learn complex relations between input parameters and performance</li></ul></li></ul>	<ul style="list-style-type: none"><li>- Interpolation level: learn accurate interpolation model and predict small-scale performance under input parameters in <math>X_{test}</math></li></ul>
<ul style="list-style-type: none"><li>- Sophisticated algorithms:<ul style="list-style-type: none"><li>· learn accurate relations between input parameters and performance</li><li>· overfitting on small-scale data</li></ul></li></ul>	<ul style="list-style-type: none"><li>- Extrapolation level: construct model owning extrapolation ability and predict <math>y_{test}</math> with corresponding small-scale performance predictions</li></ul>

# Workflow of Two-Level Model

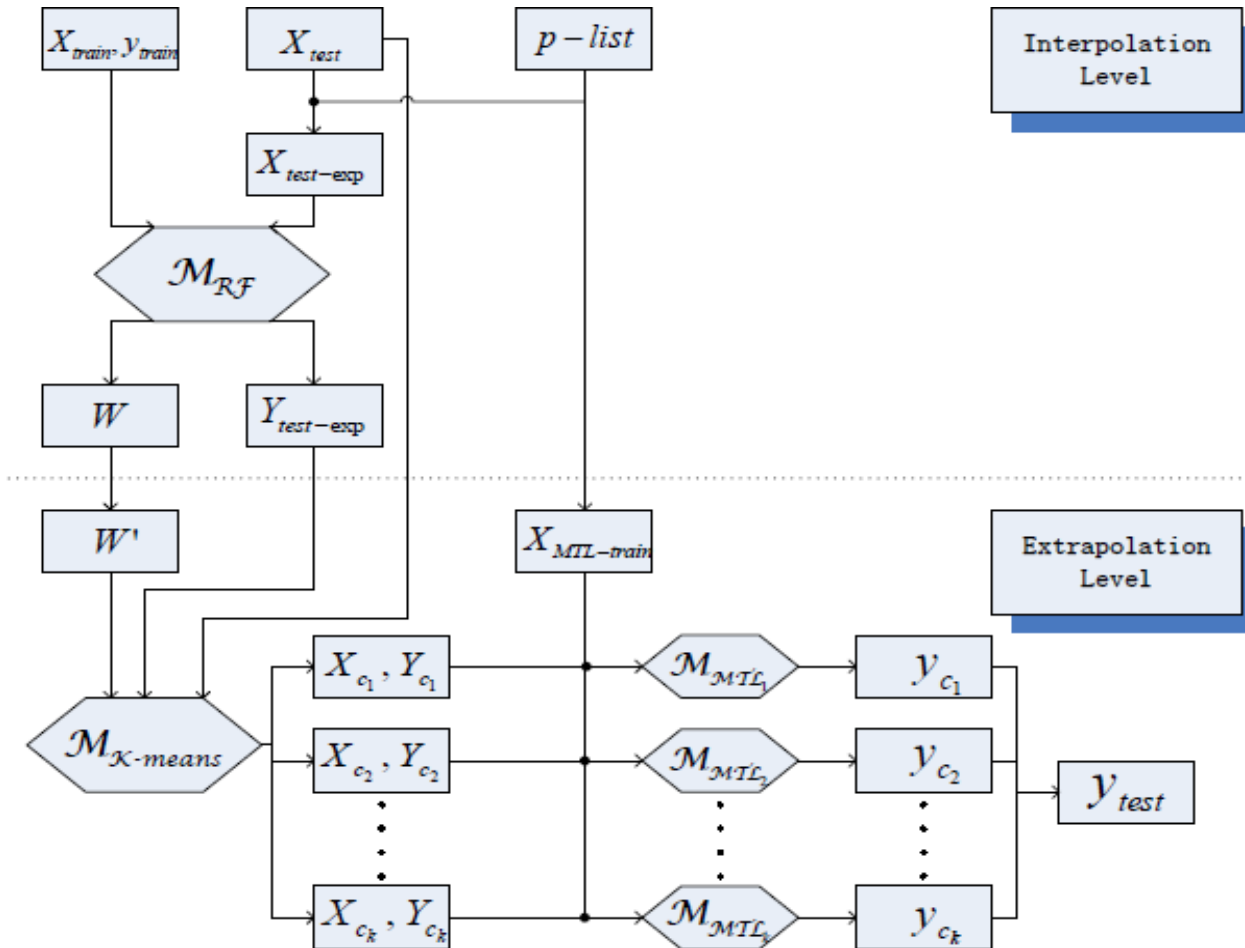
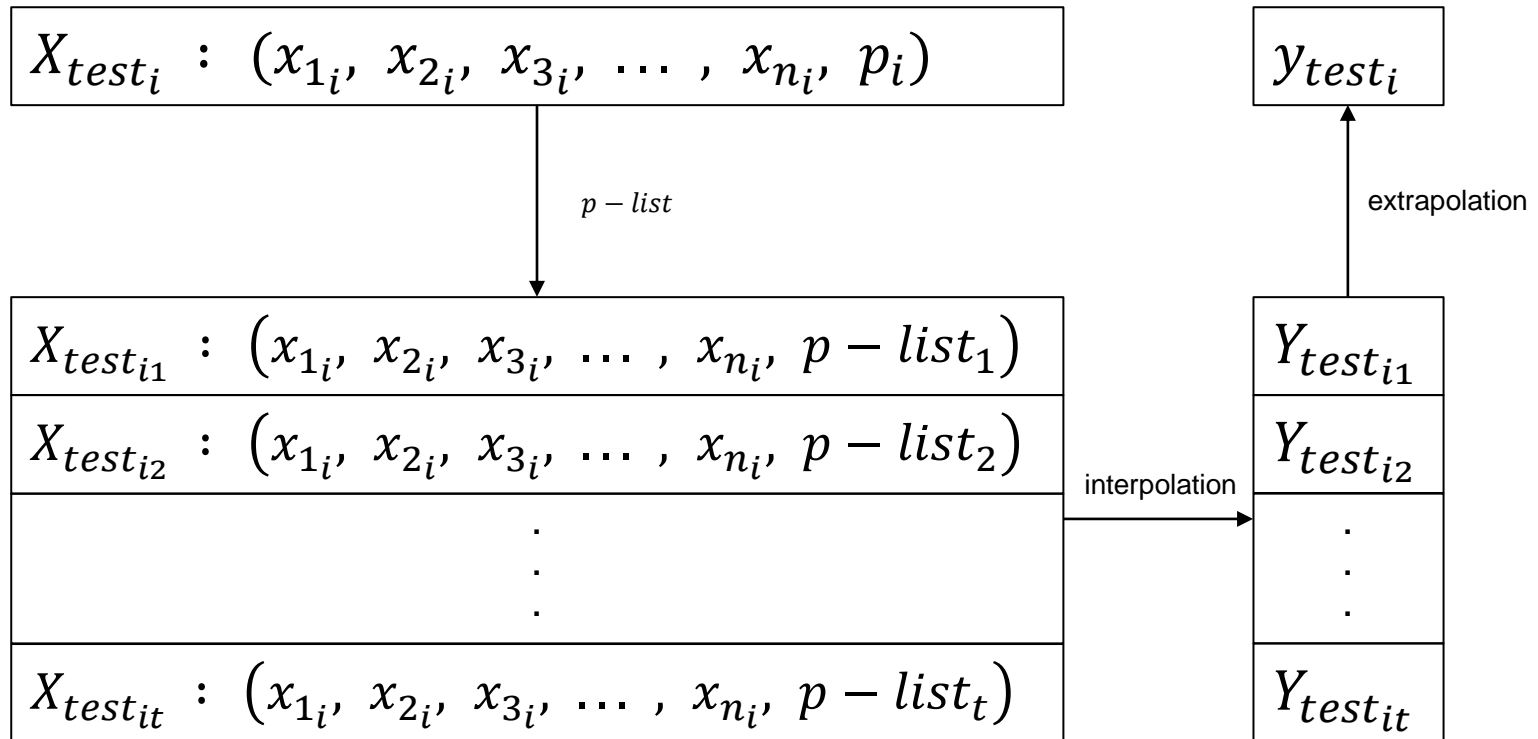


fig 3. workflow of two-level model

# Prediction Specification



# Analysis of Interpolation Level

- Task:  
small-scale performance predictions as extrapolation  
level training data
- Requirement:
  - high accuracy
  - random error distribution

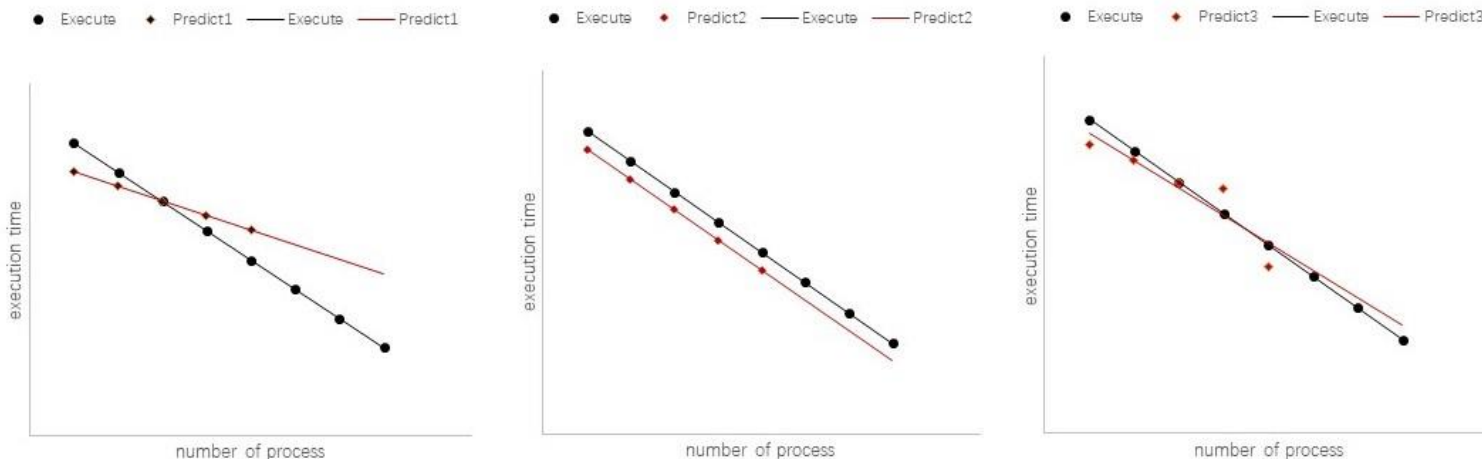


fig 4. influence of error distribution

# Interpoaltion Level Model

- feature randomness
- sample randomness

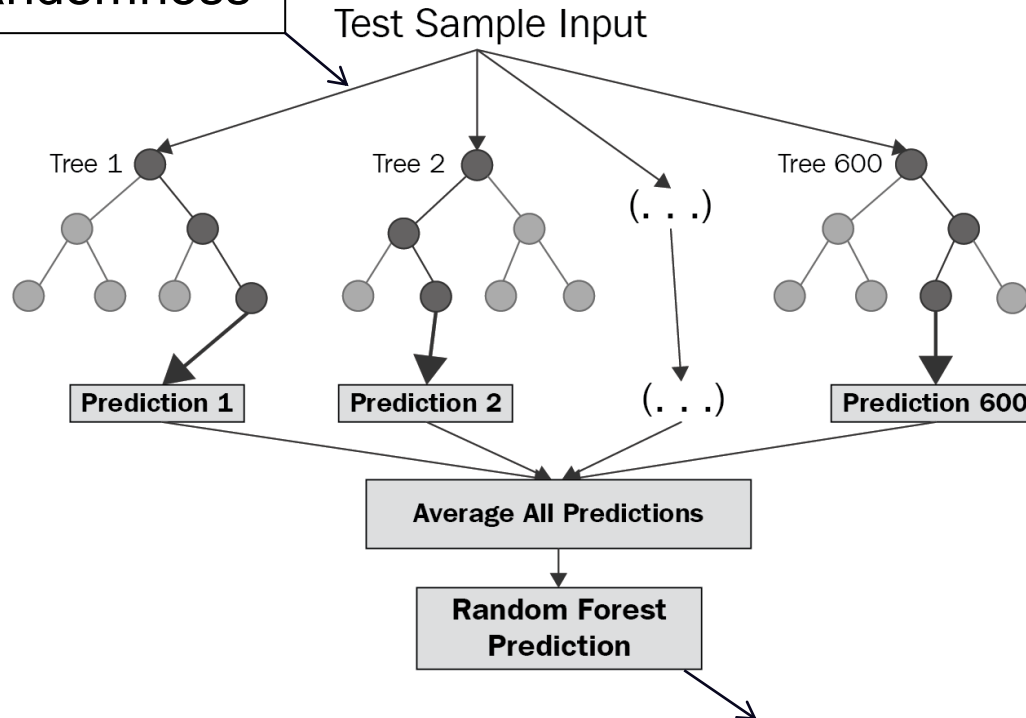


fig 5. random forest

- high accuracy
- random error distribution

# Analysis of Extrapolation Level

---

- Task:
  - predict large-scale performance with small-scale predictions
- Challenge:
  - extrapolation (scalability) — scalability may change with input parameters
  - interpolation error — only several data points for every input parameter combinations, easy to overfit causes error amplification

# Extrapolation Level Model

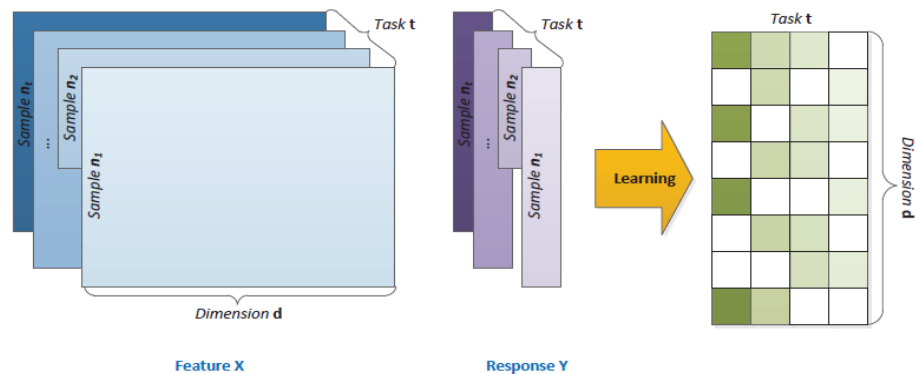
## Scalability

Performance Modeling Normal Form(PMNF):

$$f(p) = \sum_{k=1}^n c_k \cdot p^{i_k} \cdot \log_2^{j_k}(p)$$

## Interpolation Error

Multi-Task Lasso:





**03**

Experiment  
Results & Analysis

# Experiment

Platform Node	
Specification	configuration
CPU type	E5-2680 v4
CPU frequency	2.4GHz
#core	28
memory	128GB
network	100Gbps OPA

Monte Carlo Benchmark (MCB) Features		
Name	Type	Values
nZonesX	integr	[100, 1000]
nZonesY	integer	[100, 1000]
xDim	float	[1.0, 10.0]
yDim	float	[1.0, 10.0]
xSource	float	[1.0, 10.0]
ySource	float	[1.0, 10.0]
numParticles	integer	$[1 \times 10^7, 2 \times 10^7]$
#process	integer	[16, 32, 48, ..., 512]

Kripke Features		
Name	Type	Values
layout	enumeration	DGZ, DZG, GDZ, GZD, ZDG, ZGD
gset	integer	1, 2, 4, 8, 16, 32, 64, 128
dset	integer	8, 16, 32
pmethod	enumeration	sweep, bj
#process	integer	1, 2, 4, 8, 16, 32, 64, 128

# Evaluation

## Baseline

- Random Forest
- Multi-Layer Perceptron
- EPMNF

$$f(P) = \sum_{i=1}^{|P|} \sum_{k=1}^n c_i \cdot p_i^{j_{ik}} \log_2^{l_{ik}}(p_i)$$

- Log Rgression

$$\log(T) = \beta_1 \log(x_1) + \beta_2 \log(x_2) + \dots \\ \beta_n \log(x_n) + \beta_p \log(p) + error$$

## Metrics

- MAE

$$MAE = \frac{1}{n} \sum_{i=1}^n |\hat{y}_i - y_i|$$

- MAPE

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{\hat{y}_i - y_i}{y_i} \right|$$

- RMSE

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2}$$

# Result: Comparison of Different Methods

---

App	Method	MAPE		MAE		RMSE	
		inter	extra	inter	extra	inter	extra
MCB	RF	0.1481	1.4097	14.62	42.12	21.55	48.20
	MLP	0.1729	0.5323	17.06	20.64	25.15	27.88
	EPMNF	0.2560	1.2191	21.21	33.95	27.73	41.57
	LR	0.1677	0.3640	18.99	9.87	31.28	12.42
	RFMTL	0.1481	<b>0.2577</b>	14.62	<b>8.37</b>	21.55	<b>11.45</b>
Kripke	RF	0.0610	0.8676	5.63	16.11	23.55	31.63
	MLP	0.3320	0.4758	27.24	12.71	52.91	26.98
	EPMNF	0.7324	3.4028	29.77	24.79	55.87	34.07
	LR	0.3088	0.6729	25.58	17.85	55.81	41.07
	RFMTL	0.0610	<b>0.2524</b>	5.63	<b>7.74</b>	23.55	<b>20.58</b>

- extrapolations are harder than interpolations
- the performance of the same method in different applications varies greatly
- two-level model perform better than one-level model

# Result: Comparison of Different Methods

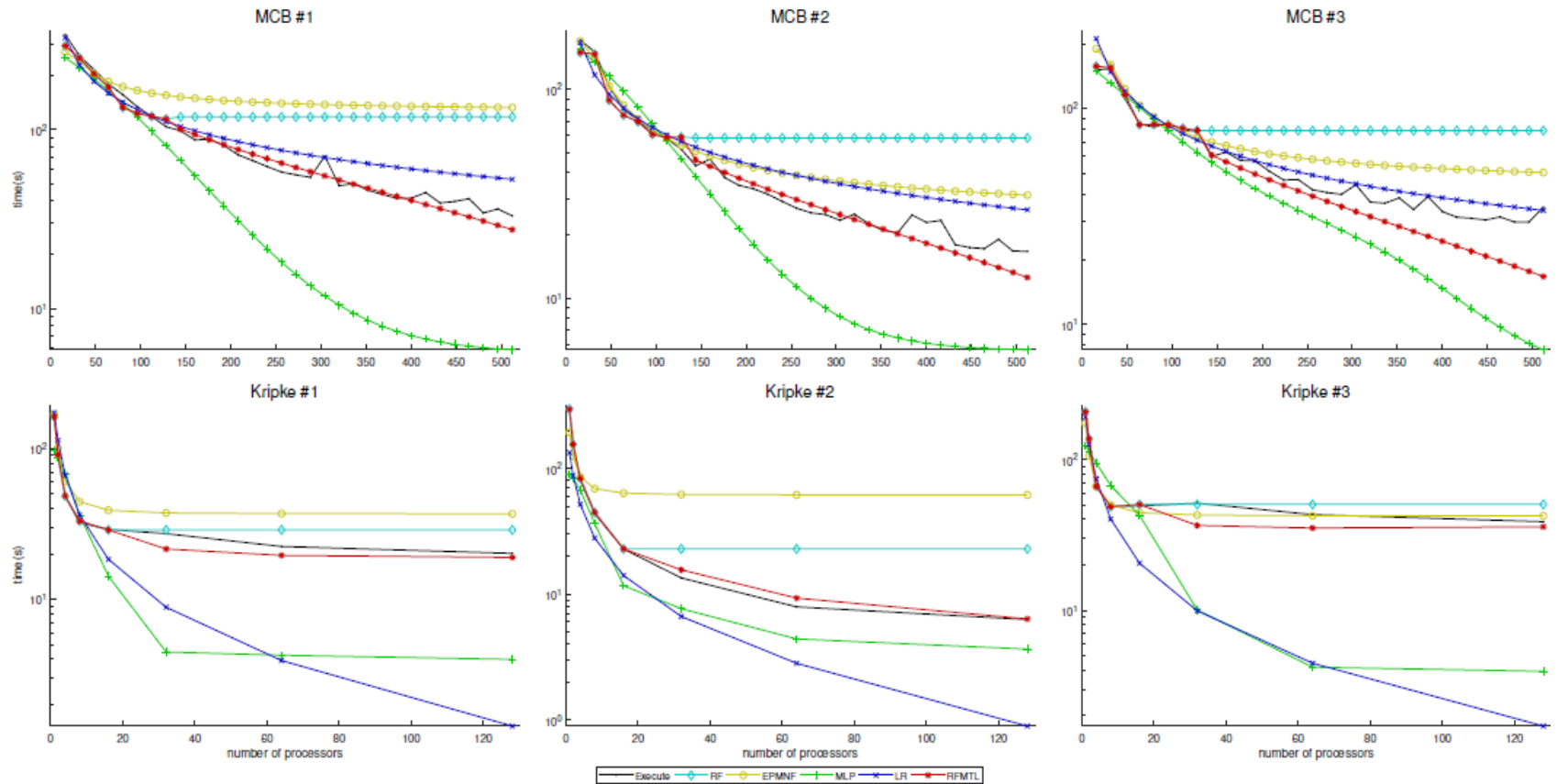


fig 6. case study of different methods

# Result: Single-Task v.s. Multi-Task

App	Method	MAPE	MAE	RMSE
MCB	ST	0.6789	28.06	61.35
	MT	<b>0.2659</b>	<b>9.77</b>	<b>14.25</b>
Kripke	ST	0.6662	17.67	41.47
	MT	<b>0.2880</b>	<b>8.12</b>	<b>18.22</b>

## Multi-Task Learning

- data amplification
- feature selection

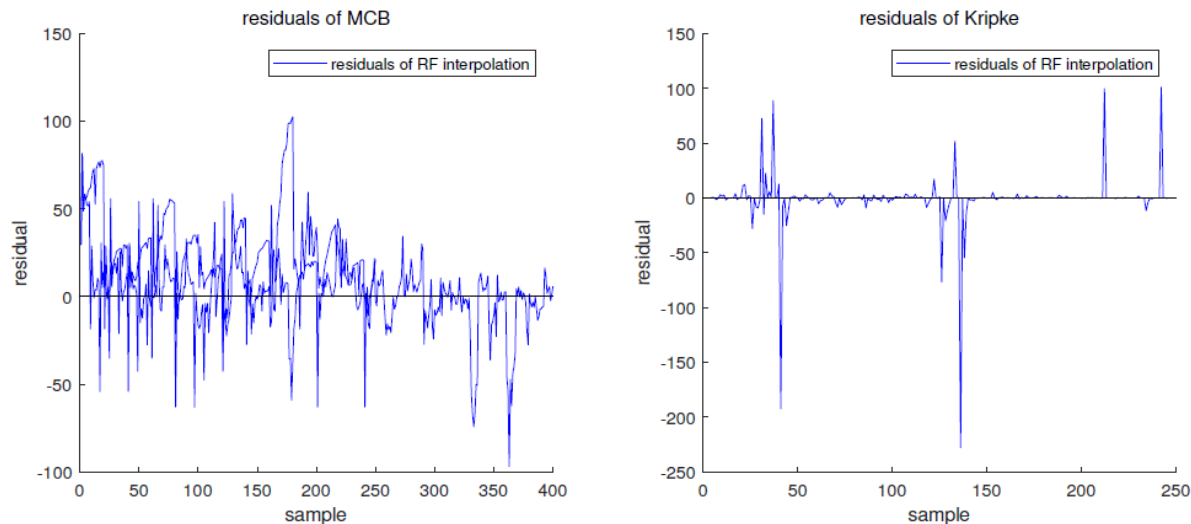


fig 7. residuals of random forest

# Result: Single-Task v.s. Multi-Task

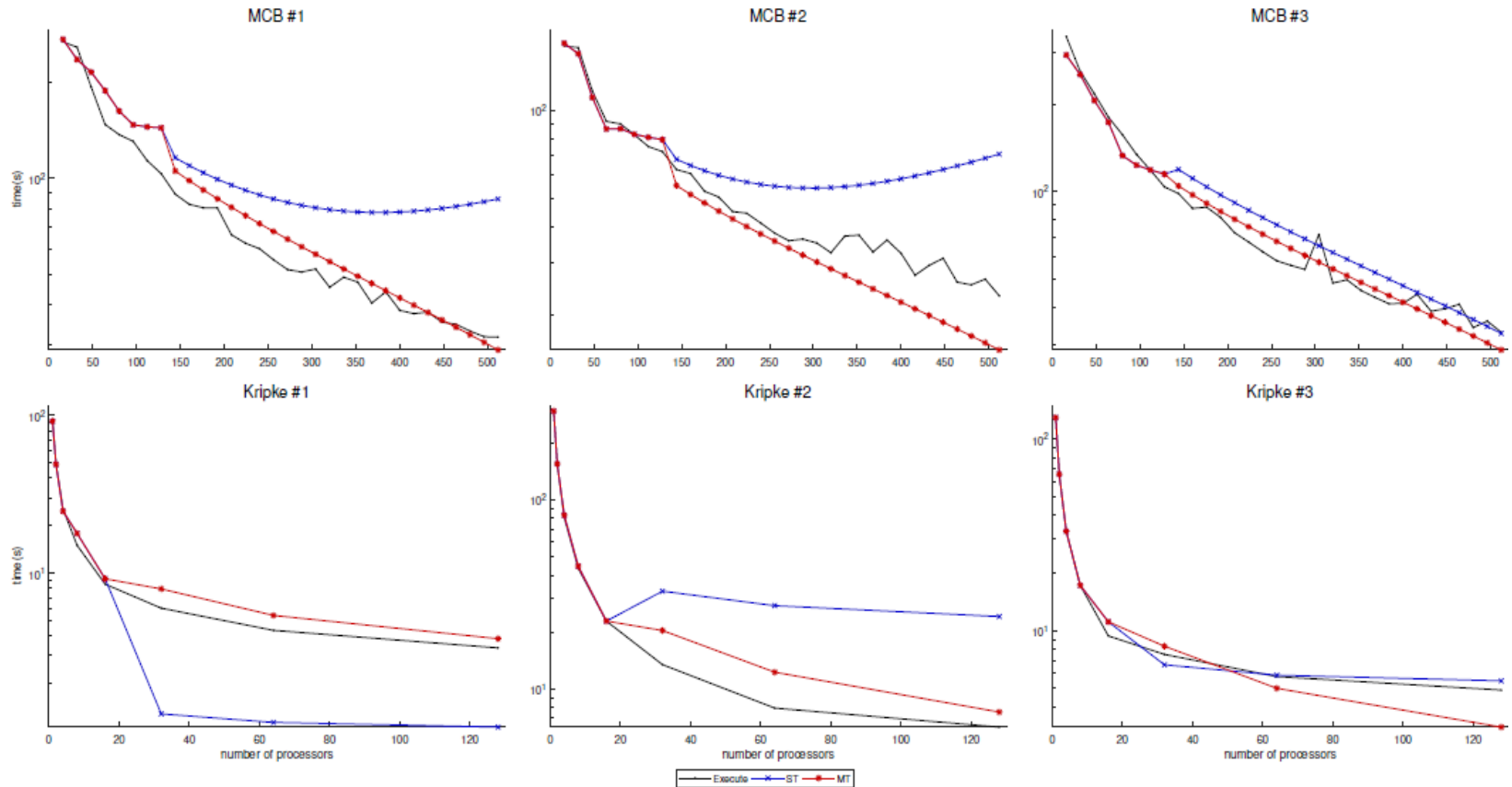


fig 8. case study of multi-task learning

# Result: Clustering or Not

## K-means Cluster

- distance:

$$Dist(X_i, X_j) = \sqrt{\sum_{k=1}^n W'_k (X_{ik} - X_{jk})^2}$$

- effect:

partition tasks into cluster by distance (relatedness) to learn high-related tasks jointly.

App	Method	MAPE	MAE	RMSE
MCB	NCL	0.2659	9.77	14.25
	CL	<b>0.2577</b>	<b>8.37</b>	<b>11.45</b>
Kripke	NCL	0.2880	8.12	<b>18.22</b>
	CL	<b>0.2524</b>	<b>7.74</b>	20.58

### reasons for insignificance

- input sensitivity
- experimental feature values range
- clustering algorithm

# Result: Clustering or Not

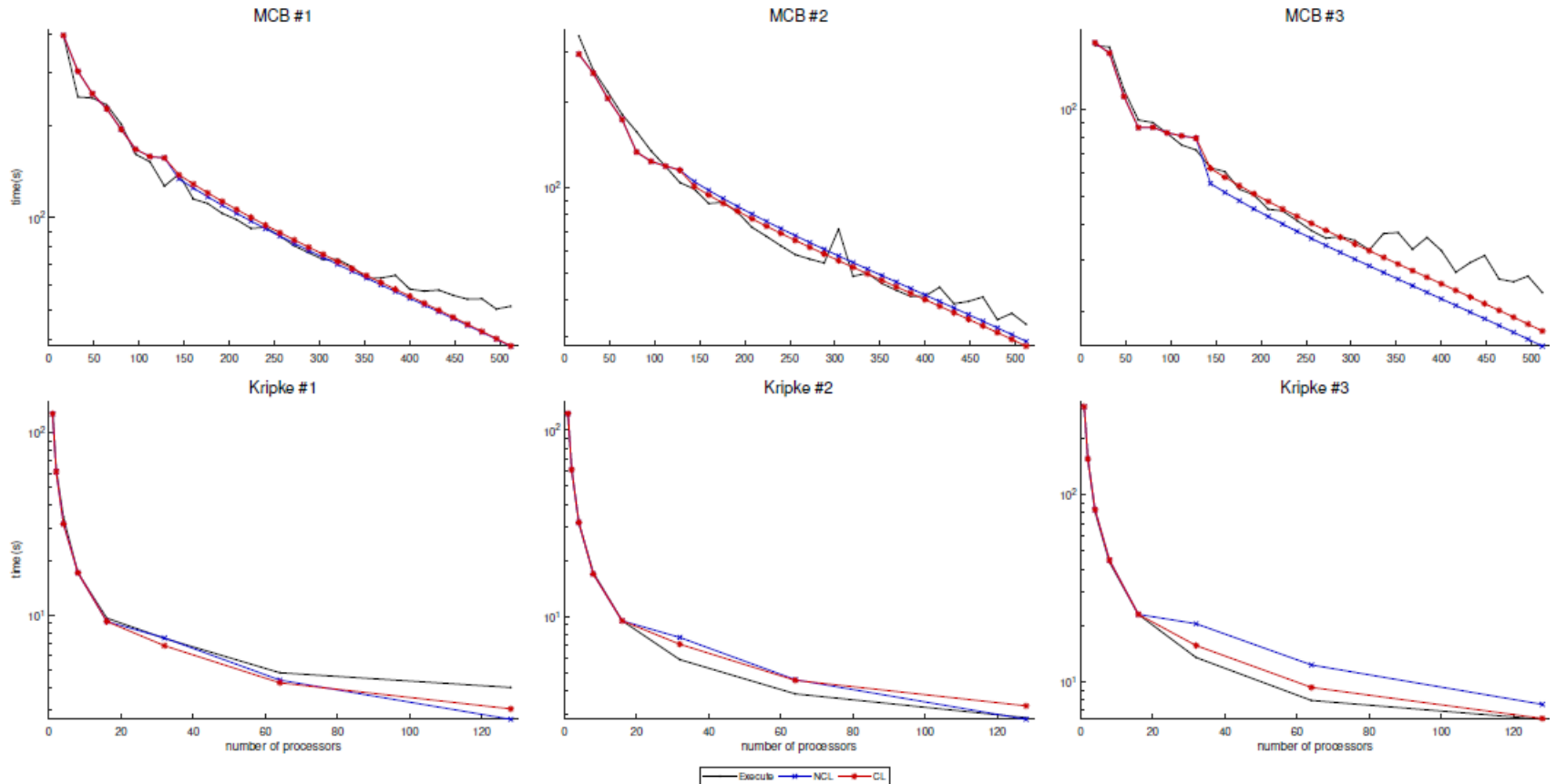


fig 9. case study of clustering



**04**

| Conclusions

# Conclusions

---

- analyze the extrapolation problem and issues of one-level model
- propose a two-level model to predict large-scale performance with only small-scale historical data
- conduct experiment to validate the effectiveness of two-level model

# Future Work

---

- improve two-level model by choosing more fitting clustering and multi-task learning algorithms
- improve scalability models with considering system information to model cross-platform performance
- research whether two-level model works for extrapolation problem caused by input parameter



**Thanks.**

Welcome further  
communication.

Wenju Zhou

zhouwenj@mail.ustc.edu.cn